ENGINEERING SCIENCE C103 EXAM SOLUTIONS 2005

Q 7 Twelve 10 k Ω resistors are connected as shown.

Determine the voltage at each node if:-

- a) a 6 V battery is connected between O and B
- b) a 6 V battery is connected between O and H



a) Because of symmetry the voltage at A D and G must be 3 V

Examining node C we may deduce the current flow is as shown since V_C must be less than 3 V Working in mA, Ohms Law gives A

$$\begin{split} I_1 &= V_C / 10 K = 0.1 \ V_C \\ I_2 &= (3 - V_C) / 20 k = 0.15 - 0.05 \ V_C \\ I_3 &= (3 - V_C) / 10 k = 0.3 - 0.1 \ V_C \\ \text{Kirchoff's rule gives} \\ I_1 &= I_2 + I_3 \end{split}$$

 $\begin{array}{l} 0.1 \ V_C \!=\! 0.15 - 0.05 \ V_C \! + \! 0.3 \! - \! 0.1 \ V_C \\ 0.25 \ V_C \! = \! 0.45 \\ V_C \! = \! 1.8 \ V \end{array}$

 $I_1 = 0.18 \text{ mA}$ $I_2 = 0.06 \text{ mA}$ $I_3 = 0.12 \text{ mA}$ We can easily deduce the other currents as shown Now use Ohms Law to find voltages.





b) Again by symmetry we can deduce that $V_G,\,V_D$ and V_A are 3V

Again examining node C we deduce the voltage is between 3 and 0 so the currents flow as shown.

$$\begin{split} I_1 &= V_C / 10 K = 0.1 \ V_C \\ I_2 &= (3 - V_C) / 10 k = 0.3 - 0.1 \ V_C \\ I_3 &= (3 - V_C) / 10 k = 0.3 - 0.1 \ V_C \\ Kirchoff's \ rule \ gives \\ I_1 &= I_2 + I_3 \end{split}$$

 $\begin{array}{l} 0.1 \ V_C = 0.3 - 0.1 \ V_C + 0.3 - 0.1 \ V_C \\ 0.3 \ V_C = 0.6 \quad V_C = 2 \ V \\ By \ symmetry \ V_A = \ 2 \ V \end{array}$

 $I_1 = 0.2 \ mA \qquad I_2 = \ 0.1 \ mA \qquad I_3 = 0.1 \ mA$

Now use Ohms Law to find voltages.

 $V_G = 3 + 0.1 \times 10 = 4 V$ By symmetry $V_E = 4 V$

