



$$D_1 = 0.15\text{m} \quad D_2 = 0.05\text{m} \quad D_3 = 0.1\text{m} \quad Q_1 = 0.05 \text{ m}^3/\text{s}$$

$$p_1 = 400 \times 10^3 \text{ N/m}^2 \quad p_2 = 395 \times 10^3 \text{ N/m}^2$$

$$A_1 = \frac{\pi D_1^2}{4} = 0.018 \text{ m}^2 \quad A_2 = \frac{\pi D_2^2}{4} = 0.001963 \text{ m}^2 \quad A_3 = \frac{\pi D_3^2}{4} = 0.007854 \text{ m}^2$$

$$u_1 = \frac{Q_1}{A_1} = 2.829 \text{ m/s}$$

CONSERVATION OF ENERGY OF A STREAMLINE FROM (1) TO (2)

$$p_1 + \rho \frac{u_1^2}{2} = p_2 + \rho \frac{u_2^2}{2}$$

$$400 \times 10^3 + 998 \frac{2.829^2}{2} = 395 \times 10^3 + 998 \frac{u_2^2}{2} = 404 \times 10^3$$

$$u_2 = 4.246 \text{ m/s}$$

$$\text{FLOW RATE} \quad Q_2 = A_2 u_2 = 0.008336 \text{ m}^3/\text{s}$$

$$\text{CONSERVATION OF MASS} \quad Q_3 = Q_1 - Q_2 = 0.042 \text{ m}^3/\text{s} \quad u_3 = \frac{Q_3}{A_3} = 5.305 \text{ m/s}$$

CONSERVATION OF ENERGY OF A STREAMLINE FROM (1) TO (3)

$$p_1 + \rho \frac{u_1^2}{2} = p_3 + \rho \frac{u_3^2}{2}$$

$$400 \times 10^3 + 998 \frac{2.829^2}{2} = p_3 + 998 \frac{u_3^2}{2} = 404 \times 10^3$$

$$p_3 = 404 \times 10^3 - 998 \frac{5.305^2}{2} = 390 \times 10^3 \text{ N/m}^2$$

FORCES

Horizontal force = $m \Delta u + A \Delta p$ in horizontal direction.

$$F_h = \rho Q_1 (0 - 2.829) + 0.018 (0 - 400 \times 10^3) = -7.21 \text{ kN} \quad (\text{To right on diagram})$$

Vertical force = $m \Delta u + A \Delta p$ in vertical direction. There are two calculations.

$$F_{v1} = \rho Q_2 (u_2 - 0) + A_3 p_3 = (998 \times 0.008336 \times 4.246) + (0.001963 \times 390 \times 10^3)$$

$$F_{v1} = 810.9 \text{ N Up}$$

$$F_{v2} = \rho Q_3 (u_3 - 0) + A_3 p_3 = (998 \times 0.042 \times 5.305) + (0.007854 \times 390 \times 10^3)$$

$$F_{v2} = 3.283 \times 10^3 \text{ N Up}$$

$$\text{Total vertical force} = 4.094 \text{ kN Up}$$

$$\text{RESULTANT FORCE} = \{4.094^2 + 7.21^2\}^{1/2} = 8.291 \text{ kN}$$