## Unit code: A/601/1625 QCF level: 4 Credit value: 15

## TUTORIAL - OUTCOME 2 Part 1

This work covers part of outcome 2 of the Edexcel standard module. The material is quite suitable for anyone wishing to study this interesting subject. This tutorial requires basic mathematical skills and a reasonable knowledge of digital electronic terminology. An industrial background will also be of great benefit to students. Obviously, access to suitable computer software such as Pneusim Pro ${ }^{\mathrm{TM}}$ or Bytronics ${ }^{\mathrm{TM}}$ simulation software will be a great help.

## SYLLABUS

## 2 Understand PLC information and communication techniques

Forms of signal: analogue (0-10 V dc. 4-20 digital
Digital resolution and relationships: 9-bit; 10-bit 12-bit
Number systems: decimal; binary; octal; hexadecimal; Binary-Coded Decimal (BCD)
Evaluate communication standards: comparison of typical protocols used in signal communication
Evaluate networking methods and standards: master to slave; peer to peer; ISO; IEE; MAP
Logic functions: writing programmes using logic functions based on relay ladder logic (AND; OR; EXCLUSIVE OR; NAND; NOR)

| Learning outcomes <br> On successful completion of this unit a learner will: | Assessment criteria for pass <br> The learner can: |
| :---: | :---: |
| L02 Understand PLC information and communication techniques | 2.1 evaluate the different forms of signal used in programmable logic control <br> 2.2 describe the resolution and relationship between analogue inputs and outputs and word length <br> 2.3 express numbers using different number systems <br> 2.4 describe typical protocols used in signal communication and evaluate networking methods and networking standards |

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## 1. INTRODUCTION

Programmable logic controllers are digital devices and using the same kind of internal structure as computers. The information is processed internally in digital forms using data and address busses. They must communicate with external devices such as other computers and programming panels. The digital communication must conform to industrial standards. In industrial applications there are many analogue signals and these must be converted into or from the digital form before they can be received or sent by the PLC.

We first need to look at digital information and how it forms numbers of various forms.

## 2. NUMBER SYSTEMS

### 2.1 BINARY NUMBERS

A number may be represented in digital form by a simple pattern. The pattern may be generated for example with a row of lights switched on by an electric current. The pattern will also exist in the wires connected to the light bulbs. In digital electronics the pattern exists as a voltage relative to zero. Ideally in a typical computer, 5 V is ON or high and zero is OFF or low but to make a clear distinction, a voltage of over 3 is regarded high and below 2 is regarded as low. The patterns were originally developed in computers for 8 lines and then this became 16,32 and 64 . Consider a pattern of 8 lines. We indicate on or high with a 1 and off or low with a 0 . Each line carries a bit of information as on or off and so the line is referred to as a bit.

In the denary system the digit that represents the highest value is on the left (e.g. the 3 in 32 or the 4 in 461). The digit representing the lowest value is on the right. These are called the most significant digit and least significant digit. In binary numbers we adopt the same idea with the bit on the left being the most significant bit (MSB) and the one on the right being the least significant bit (LSB).


Figure 1
The total pattern is called a word and the one shown is an 8 bit word. The pattern may be stored in a register so it is also referred to as an 8 bit register. A register is a temporary store where the word may be manipulated.

Each bit has a value of zero when off (low) or the denary value shown when on (high). The denary value of the pattern is found by adding them all up. The maximum value for an 8 bit word is when all the bits are high and corresponds to 255 . The minimum value is 0 when they are all low so there are 256 possible values.

## WORKED EXAMPLE No. 1

What is the denary value of the digital pattern below?


Figure 2

## SOLUTION

$128+64+8+2=202$

## SELF ASSESSMENT EXERCISE No. 1

Write down the decimal value represented by the following 8 bit patterns.
10101011 $\qquad$
10010010 $\qquad$
01001011 $\qquad$

Here is a small table of binary numbers with the equivalent denary values.

| BINARY |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 00 | 01 | 10 | 11 | 100 | 101 | 110 | 111 | 1000 | 1001 | 1010 | 1011 | 1100 | 1101 | 1110 | 1111 |
| DENARY |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |

## CONVERSION

A way of converting decimal into binary is to keep dividing the number by 2 as follows.
Convert decimal 12 into binary form.

| $12 \div 2=6$ | remainder 0 |
| ---: | :--- | ---: |
| $6 \div 2=3$ | remainder 0 |
| $3 \div 2=1$ | remainder 1 |
| $1 \div 2=0$ | remainder 1 |

The binary pattern is hence 1100

Another way to express the value of each bit comes about by realising that each bit is 2 raised to the power of the bit number.


Figure 3

### 2.2. OCTAL and HEXADECIMAL

Octal is a numbering system based on cycles of 8 . It is quite easy to convert a digital number into octal and for this reason it is used by programmers to address memory locations and port addresses (printer port, com port, CD driver address and so on). Early computers used words with 8 bits so octal was convenient to use.

Hexadecimal is a numbering system based on 16 and was introduced for the same reasons as octal when computers were developed with 16 bit registers. Hexadecimal Numbers are of far greater importance in modern computing. One Nibble (4 bits) is represented by 1 Hex digit. One Byte is represented by 2 Hex Digits.

In octal we have no need for the figures 9 as the cycle restarts after 7 .
In hexadecimal, we need extra figures and the letters $\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}, \mathrm{E}$ and F are used.
Here is the beginning of a conversion table:

| Decimal | Binary | Octal | Hexadecimal |
| :--- | :--- | :--- | :--- |
| 0 | 00000 | 0 | 0 |
| 1 | 00001 | 1 | 1 |
| 2 | 00010 | 2 | 2 |
| 3 | 00011 | 3 | 3 |
| 4 | 00100 | 4 | 4 |
| 5 | 00101 | 5 | 5 |
| 6 | 00110 | 6 | 6 |
| 7 | 00111 | 7 | 7 |
| 8 | 01000 | 10 | 8 |
| 9 | 01001 | 11 | 9 |
| 10 | 01010 | 12 | A |
| 11 | 01011 | 13 | B |
| 12 | 01100 | 14 | C |
| 13 | 01101 | 15 | D |
| 14 | 01110 | 16 | E |
| 15 | 01111 | 17 | F |
| 16 | 10000 | 20 | 10 |
| . | $\cdot$ | . | . |
| . | . | . | . |
| . | . | . | . |

### 2.3 CONVERSION TO/FROM BINARY

Whereas Decimal seems to have no connection with Binary, from this table we can see that Octal and Hexadecimal are linked to Binary. The first digit in Octal corresponds to the first three digits in it's Binary equivalent, and so on. The same is true for Hexadecimal, but this time each digit represents four Binary digits.
(It may be useful to note that $8=2^{3}$, and $16=2^{4}$ ).
An advantage of knowing this is that is makes conversion to/from Binary very easy.

## WORKED EXAMPLE No. 2

Convert :1111101 Into Octal and Hexadecimal

## SOLUTION

## Octal:

Split the number into groups of 3 starting from the L.S.B. on the right.

## 1111101

Now convert each group immediately into one Octal digit, i.e. 1 becomes 1,111 becomes 7, 101 becomes 5 .

So $: 1111101=$ ( $@ 175$ is the prefix indicating an Octal number)

## Hexadecimal:

Split the number into groups of 4 starting on the right.
1111101
Convert each group immediately into one Hex digit, i.e. 111 becomes 7, 1101 becomes D.
So $: 1111101=\& 7 \mathrm{D} \quad$ ( $\&$ is the prefix indicating a Hexadecimal number)

Conversion from Octal and Hexadecimal to Binary is similarly easy.

### 2.4 DECIMAL TO OCTAL CONVERSION

This is done in a similar way to converting Decimal to Binary. Repeatedly divide the decimal number by 8 and read off the remainders in reverse order.

## WORKED EXAMPLE No. 3

Convert 70 Into Octal.

## SOLUTION

$70 \div 8=8$
Remainder 6
$8 \div 8=1$ Remainder 0
$1 \div 8=0$
Remainder 1
So $70=@ 106$

## WORKED EXAMPLE No. 4

Convert 125 into Octal

## SOLUTION

$125 \div 8=15 \quad$ Remainder 5
$15 \div 8=1 \quad$ Remainder 7
$1 \div 8=0 \quad$ Remainder 1
So $125=@ 175$

### 2.5 DECIMAL TO HEX CONVERSION

This again is done by repeatedly dividing the Decimal number by 16 and reading off the remainders in reverse order.

## WORKED EXAMPLE No. 5

## Convert 70 into Hexadecimal

## SOLUTION

| $70 \div 16=4$ | Remainder 6 |
| :--- | :--- |
| $4 \div 16=0$ | Remainder 4 |
| So $\quad 70=\& 46$ |  |

## WORKED EXAMPLE No. 6

## Convert 125 into Hexadecimal

## SOLUTION

```
125\div16=7 Remainder D
7\div16=0 Remainder 7
So 125 = &7D
```

An application of Hexadecimal numbers is for representing bit patterns. For example the letter "A" is represented in ASII codes as 01000001 or more conveniently \& 41 . Similarly, the letter " B " is represented as \&42.

## SELF ASSESSMENT EXERCISE No. 2

1. Convert 45 into Hex.
2. Convert 20 into Octal
3. Convert 125 into Binary.

Note that most scientific/engineering calculators are able to do these conversions.

### 2.6. APPLICATIONS

Consider the basic operation of a computer memory ship. The chip has an address bus and a data bus. It also has a read or write command
 line.

Each line in the bus can be on (high) or off (low) so the system is based on binary patterns. Older equipment had 8 lines in each bus and so Octal became useful. Later this increased to 16 lines so hexadecimal became useful. It has since moved on to 32 and 64 lines.

Clearly to use larger numbers, you need more lines in the bus.
Figure 4
The diagram shows 8 lines in each bus. When they are all low the decimal value is 0 . When they are all high the decimal value is 255 so there are 256 different values that can be represented.

When the $\mathrm{R} / \mathrm{W}$ line is set to write, the binary pattern on the data bus is transferred into a store at the address represented by the binary pattern on the address line. This store is also called a register and the binary pattern is contained in this register.

When the $\mathrm{R} / \mathrm{W}$ line is set to read, the pattern stored in the register at the address on the address bus is transferred to the data bus.

## SELF ASSESSMENT EXERCISE No. 3

Write down the data value in decimal and the address in octal for the case shown.


Figure 5

### 2.7. MANIPULATION

Numbers stored in registers may be added or subtracted to a number stored in another register. This is done in a processing chip. The number from two memory locations is transferred into data registers. A command to the processor makes it add them and the result is placed in a third data register and perhaps transferred to a memory location.

## ADDING IN DECIMAL

## 235+

926
1161

Starting with the LSB $5+6=11 \quad$ write down 1 carry 1
Next $\quad 3+2+$ carry $1=6$ write down 6 carry 0
Next $\quad 2+9+$ carry $0=11$ write down 1 carry 1
Next start a new column and write down carry 1

## ADDING IN BINARY

The process is the same.
$01101101+$
$\frac{11011001}{101000110}$

| Starting the LSB, | $1+1=10$ | write down 0 carry 1 |
| :--- | :--- | :--- |
| Moving to bit 1 | $0+0+$ carry $=1$ | write down 1 carry 0 |
| Moving to bit 2 | $1+0+$ carry $0=1$ | write down 1 carry 0 |
| Moving to bit 3 | $1+1+$ carry $0=10$ | write down 0 carry 1 |
| Moving to bit 4 | $0+1+$ carry $1=10$ | write down 0 carry 1 |
| Moving to bit 5 | $1+0+$ carry $1=10$ | write down 0 carry 1 |
| Moving to bit 6 | $1+1+$ carry $1=11$ | write down 1 carry 1 |
| Moving to bit 7 | $0+1+$ carry $1=11$ | Write down 1 carry 1 |

Moving to bit 8 which does not exist there is an implied $0+0+$ carry 1 so write down 1 . Clearly to store this number you would need a register with more than 8 bits.

## ADDING IN OCTAL

This is similar but remember that it is based on 8 .
$332+$
$\underline{167}$
521
Starting with the LSB
$2+7=11$
write down 1 carry 1
Next
$3+6+$ carry $1=12$
write down 2 carry 1
Next $3+1+$ carry $1=5$ write down 5

Adding in HEX is more difficult as you need to remember the values of ABCDEF
It is best to do it on the calculator. Computers do it in binary and the answers are usually expressed in Decimal, Octal or Hex.

## SELF ASSESSMENT EXERCISE No. 4

Use your calculator to do the following calculations.

| Binary | Octel | Hexadecimal |
| :--- | :--- | :--- |
| $11011 \times 01101=$ | $@ 27 \times @ 35=$ | $\& 2 \mathrm{D} 5 \times \& 3 \mathrm{~A} 1=$ |
| $11100+101100=$ | $@ 326+@ 667=$ | $\& 5 \mathrm{CE}+\& 9 \mathrm{EF}=$ |
| $11000-01011=$ | $@ 642-@ 341=$ | $\& \mathrm{FF} 5-\& 3 \mathrm{DE}=$ |

### 2.8. BINARY DECIMAL CODES

BCD is yet another way of presenting digital data as a number and it is used in industrial applications (e.g. to code or decode a digital signal from a position transducer).

The digital pattern in a register is converted into a 3 digit BCD as follows. The first 4 bits are turned into a normal (denary) number and this number is the units. The next 4 bits are the tens and the next 4 bits are the hundreds. The units cannot exceed a total of 9 . The tens cannot exceed a total of 90 and the hundreds cannot exceed a total of 900 . The maximum number which can be represented is 999.

## WORKED EXAMPLE No. 7

Deduce the value of the BCD pattern.

```
3 digit \(B C D\)


Figure 6

\section*{SOLUTION}

The first 4 bits decode to \(4+2=6\)
The second 4 bits decode to \(2+1=3\)
The third 4 bits decode to \(4+1=5\)
The decimal value represented is hence 536

\section*{SELF ASSESSMENT EXERCISE No. 5}

Deduce the value of this BCD pattern


Figure 7
Answer 695

\section*{3. REGISTERS}

A register is a memory location containing a digital number. The difference between a register and any other memory location is that the bits may be manipulated under control of the programme. Hence the bits may be shifted right or left or rotated. Depending on the programme, the new bit may be a 1 or a 0 .

\section*{SHIFTING}

Consider the example below where the register is shifted right with a 1 being added.

\section*{}

What is the decimal value before the shift? \(\qquad\)
What is the decimal value after the shift? \(\qquad\)
Now consider the same problem with a left shift.


What is the decimal value before the shift? \(\qquad\)
What is the decimal value after the shift? \(\qquad\)
Each bit of the register may be used to control an output so if a bit changes from 0 to 1 the output connected to the bit is turned on. There are many uses for shifting; one of them is to produce a counter.

\section*{ROTATING}

Rotating is similar to shifting but the bit that drops off the end reappears as the new bit.


\section*{1] \(0110|1| 0 \mid 10\)}

Numbers stored in registers can be manipulated.

\section*{ADDING and SUBTRACTION}

The contents of one register are added or subtracted to/from the contents of another and the result placed in a third register.

\section*{MULTIPLICATION and DIVISION}

The contents of one register may be multiplied or divided by the contents of another and the result placed in a third register.

\section*{INCREMENTING AND DECREMENTING}

The decimal value of the register is increased by 1 when incremented and decreased by 1 when decremented.

\section*{COMPARISON}

The contents of two registers may be compared to see if they are the same.
Other arithmetical operations may be done such as square roots and differentiation depending on the PLC. The actual operation is much more complicated than discussed here and the result leads to carry over or borrowing of bits. There are special flags that are switched on to indicate these things.

FLAGS are single bits in a register that are switched on to indicate the status of something. They are not physical outputs. They can be addressed and used within a programme. PLCs often contain flags that are automatically switched on when a certain event happens such as illustrated below.


Figure 8

The contents of register D1 is compared to the contents of register D2. In the process, if D1>D2 flag F1 is automatically set.
When flag 1 is set, data register 3 is incremented.

\section*{4. ANALOGUE TO DIGITAL and DIGITAL TO ANALOGUE CONVERSION}

Analogue to digital conversion is a process of turning an analogue voltage or current into a digital pattern that can be read by a computer and processed.

Digital to analogue conversion is the reversed process.
A typical module for a PLC is shown below. There are two A/D channels and one D/A channels. The module is connected to the PLC by a ribbon cable or plugs directly to the PLC.


Figure 9
The analogue signals are 4 to 20 mA in a modern system but \(0-10\) volts is still common and others are possible such as -5 V to +5 V . The appropriate signal must be connected to the appropriate terminal (V for Volts, I for current and C common). To read an analogue signal into the PLC a routine must be executed within the programme to read the appropriate input. The module produces the conversion and the digital number representing the analogue signal is read into a designated register of the PLC.

To produce an analogue output, a routine must be executed to take a digital value in a designated register and put it out to the module where it is converted into a voltage or current.

\section*{RESOLUTION}

When a digital number is converted into a voltage, each increment of the binary value corresponds with an increment in the voltage output. The value of this increment is the resolution.

Consider an 8 bit system. The minimum and maximum number that can be stored is 0 and 255 so there are 255 steps. An analogue voltage in the range 0 to 10 V van be divided up into 255 steps so the resolution is \(10 / 255=0.0392 \mathrm{~V}\). This is adequate for most purposes but if very small changes in voltages are to be detected, a higher resolution is needed. A/D and D/A systems commonly available use anything from 4 bits to 32 bits depending on the resolution required. For example if a thermocouple is used to measure temperature, the voltage change for \(1^{\circ} \mathrm{C}\) is very small and a fine resolution is needed. Other instruments fall in this category. Digital Analogue Converters (DACs) are usually on a single chip and commonly have 9,10 or 12 bit resolution.


Figure 10
10 bit DAC chip and technical specification

10BIT DAC DUAL
Resolution (Bits): 10bit
Sampling Rate: 93kSPS
Input Channel Type: Serial
Supply Voltage Range: 2.7 V to 5.5 V
Digital IC Case Style: SOIC
No. of Pins: 8
Data Interface: 3 Wire, Serial
Supply Current: 1.6 mA
Operating Temperature Min: \(-40^{\circ} \mathrm{C}\)
Operating Temperature Max: \(85^{\circ} \mathrm{C}\)
SVHC: No SVHC (19-Dec-2012)
Base Number: 5617
IC Case Style: SOIC
IC Generic Number: 5617
Input Type: Serial
Linearity Error: 0.1\%
Linearity Error ADC / DAC +: 0.5LSB
Linearity Error ADC / DAC -: 0.5LSB
No. of Bits: 10
No. of Channels: 2
No. of DACs: 2
Operating Temperature Range: \(-40^{\circ} \mathrm{C}\) to \(+85^{\circ} \mathrm{C}\)
Output Type: Voltage
Package / Case: SOIC
Sample Rate: 0.093MSPS
Sample Rate: 93 kSPS
Settling Time: \(2.5 \mu \mathrm{~s}\)
Supply Voltage Max: 5.5 V
Supply Voltage Min: 2.7V
Supply Voltage Range - Analogue: 2.7 V to \(3.3 \mathrm{~V}, 4.5 \mathrm{~V}\) to 5.5 V
Supply Voltage Range - Digital: 2.7 V to \(3.3 \mathrm{~V}, 4.5 \mathrm{~V}\) to 5.5 V
Termination Type: SMD

\section*{WORKED EXAMPLE No. 8}

An analogue instrument produces a variable voltage of 0 to 10 V . It is processed with an \(\mathrm{A} / \mathrm{D}\) converter using 5 bits. Calculate the minimum change in voltage that can be detected.

\section*{SOLUTION}

5 bits has maximum value of \(1+2+4+8+16=31\) so the smallest voltage detectable is \(10 / 31=0.322 \mathrm{~V}\)

\section*{SELF ASSESSMENT EXERCISE No. 6}

An analogue instrument produces a signal with a range 4 to 20 mA . It is processed with a 9 bit \(\mathrm{A} / \mathrm{D}\) converter. What is the smallest current change that ca be detected.

Answer 0.0313 mA```

