The diagram shows a crank handle for turning a machine. It is made from solid round bar 15 mm diameter.


## 100 mm

(a) Calculate the force required at point P so that a torque of 50 Nm is exerted on the machine.

## SOLUTION

The force has a turning arm of 150 mm so the torque is $\mathrm{T}=50=\mathrm{F} \times 0.15 \mathrm{~F}=50 / 0.15=333.3 \mathrm{~N}$
(b) Calculate the maximum principal stress produced in the handle by this force ignoring stress concentrations.

## SOLUTION

At the point where the handle is connected to the machine the bending moment is a maximum and the torque is a maximum so this point will be used.
$\mathrm{T}=50 \mathrm{Nm} \quad \mathrm{M}=333.3 \times 0.3 \mathrm{~m}=100 \mathrm{Nm}$
BENDING STRESS
$\sigma=\mathrm{My} / \mathrm{I} \quad \mathrm{y}=7.5 \times 10^{-3} \mathrm{~m} \quad \mathrm{I}=\pi \times\left(15 \times 10^{-3}\right)^{4} / 64=7.705 \times 10^{-8} \mathrm{~m}^{4}$
$\sigma=100 \times 7.5 \times 10^{-3} / 7.705 \times 10^{-8}=9.734 \times 10^{6} \mathrm{~N} / \mathrm{m}^{2}$
TORSIONAL STRESS
$\tau=\mathrm{TR} / \mathrm{J} \quad \mathrm{R}=0.15 \quad \mathrm{~J}=2 \mathrm{I}$
$\tau=50 \times 0.15 / 1.541 \times 10^{-7}=2.433 \times 10^{6} \mathrm{~N} / \mathrm{m}^{2}$
Constructing Mohr's circle of stress we get


The greatest principal stress is $\sigma_{p}=9.734 / 2+\sqrt{ }\left[2.433^{2}+(9.734 / 2)^{2}\right]=31 \mathrm{MPa}$

